



Christoph Weidenbach

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Tutorials for “Automated Reasoning WS18/19”
Exercise sheet 1

Exercise 1.1:

Determine which of the following formulas are valid/satisfiable/unsatisfiable using propositional semantics, i.e., the definition of \models :

1. $(P \wedge Q) \rightarrow (P \vee Q)$
2. $(P \vee Q) \rightarrow (P \wedge Q)$
3. $\neg(P \rightarrow \neg P)$
4. $(P \vee \neg Q) \wedge \neg(\neg P \rightarrow \neg Q)$
5. $\neg(P \vee Q) \leftrightarrow (\neg P \wedge \neg Q)$

Exercise 1.2:

Prove the validity of the following formulas using \Rightarrow_T .

1. $(P \rightarrow (Q \rightarrow R)) \rightarrow ((P \rightarrow Q) \rightarrow (P \rightarrow R))$
2. $(P \rightarrow Q) \rightarrow ((R \vee P) \rightarrow (R \vee Q))$

Exercise* 1.3:

Consider a satisfiable formula ϕ with $\mathcal{A} \models \phi$.

1. Prove \Rightarrow_T to be strongly complete with respect to models: if $\{(\phi)\} \Rightarrow_T^* N$ and N is a normal form then there is a sequence $(\phi, \phi_1, \dots, \phi_n) \in N$ such that $\mathcal{A} \models \phi \wedge \phi_1 \wedge \dots \wedge \phi_n$.
2. Is \mathcal{A} the only model of $\phi \wedge \phi_1 \wedge \dots \wedge \phi_n$?

It is not encouraged to prepare joint solutions, because we do not support joint exams.